## OBJECTIVE

1. I can determine the inverse of a function given in multiple forms.

NOTES Inverse Functions: functions in which all input and output pairs are reversed. The inverse of $f(x)$ is denoted $f^{-1}(x)$. Inverse functions have the following properties:

- $\quad f$ and $f^{-1}$ are reflections of each other across the line $y=x$.
- For every point $(a, b)$ on $f$, there is a point $(b, a)$ on $f^{-1}$.
- The domain of $f$ is the range of $f^{-1}$; the range of $f$ is the domain of $f^{-1}$.
- Both functions must be one-to-one*.
*ONE-TO-ONE FUNCTION: a function that, when graphed, passes the horizontal line test.

Note that a function such as $f(x)=x^{2}$, which is not one-toone, can be made one-to-one by restricting its domain. For example, $f(x)=x^{2}, x \geq 0$ is now a one-to-one function.

## Sters for Finding the Inverse Function

1. Substitute $x$ for $f(x)$, substitute $y$ for $x$.
2. Solve for $y$.
3. Substitute $f^{-1}(x)$ for $y$.
4. Check for necessary domain restrictions.

EXAMPLES
Find the Inverse:
$1 f(x)=5 x+7$
$2 f(x)=x^{2}-6 x+13$ when $x \leq 3$.
3. $f(x)=\frac{4 x+3}{3 x-1}$
4.

| $x$ | $f(x)=x^{3}-4 x+1$ |
| :---: | :---: |
| -7 | -314 |
| -6 | -191 |
| -5 | -104 |
| -4 | -47 |
| -3 | -14 |
| -2 | 1 |
| -1 | 4 |


6. Find a domain that will make this function invertible.
$f(x)=x^{2}-4 x-1$

Find the inverse of each function.

1. $f(x)=-6 x+8$
2. $f(x)=3 x-5$
3. $f(x)=x^{2}-4 x-12, x \geq 2$
4. $f(x)=\sqrt{x+4}$
5. $f(x)=\frac{3 x+5}{x-1}$
6. $f(x)=\frac{7 x-6}{3 x+2}$
7. $f(x)=\frac{1}{2} x^{3}-3$
8. $f(x)=(x-2)^{3}+5$
9. $f(x)=-2 \sqrt[3]{x-5}+7$
10. a.

| $x$ | $f(x)$ |
| :---: | :---: |
| -2 | 0.5 |
| -1 | 1.5 |
| 0 | 4.5 |
| 1 | 13.5 |
| 2 | 40.5 |

b.

| $x$ | $f(x)$ |
| :---: | :---: |
| 5 | 1 |
| 6 | 3 |
| 9 | 4 |
| 14 | 5 |
| 21 | 6 |

11. a.

b.

c.

| $x$ | $f(x)$ |
| :---: | :---: |
| -17 | 1.7 |
| -12 | 1.6 |
| -9 | 1.5 |
| -7 | 1.4 |
| -3 | 1 |

c.


For each function find a domain that will make the function invertible.
12. $f(x)=2 x^{2}-3$
13. $f(x)=(x+5)^{2}+4$
14. $f(x)=x^{2}+12 x+32$

