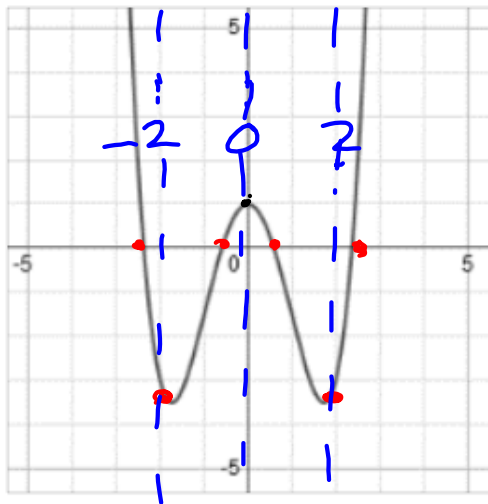


Bellwork: Identify the features listed for the graph



Increasing interval(s)  $(-2, 0)$   $(2, \infty)$

Decreasing interval(s)  $(-\infty, -2)$

Relative maximum(s)  $(0, 2)$   $(0, 1)$

Relative minimum(s)  $(-2, -3.5)$   $(2, -3.5)$

x-intercept(s)  $(-2.5, 0)$   $(0, 0)$   $(2.5, 0)$

y-intercept  $(0, 1)$   $(.5, 0)$   $(2.5, 0)$

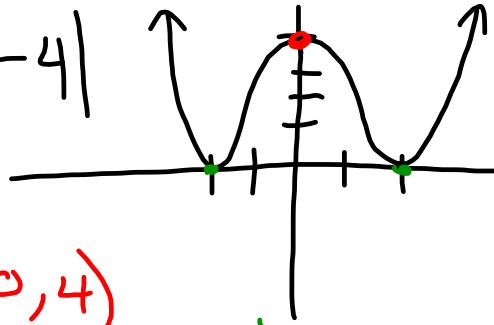
Bellwork: Classify the functions below as even, odd, or neither.

$$f(x) = 2x^2 + 4x + 3 \quad \text{neither}$$

$$f(x) = 4x^2 + 7x^0 \quad \text{even}$$

$$f(x) = 3x^5 - 2x^3 + 4x^1 \quad \text{odd}$$

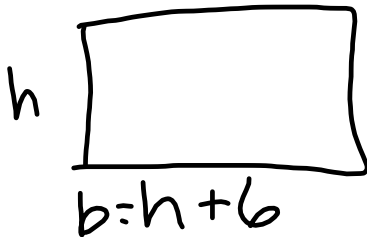
11)  $|x^2 - 4|$



max:  $(0, 4)$   
min:  $(-2, 0)$   $(2, 0)$

math  $\rightarrow$  NUM  
1. abs

8)



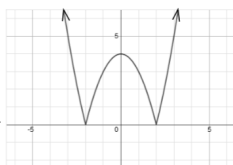
$$A = h(h + 6)$$
$$A(h) = h^2 + 6h$$

Homework 2.2 Solutions

1.
  - a. 41
  - b. -19
  - c.  $-8n - 11$
2.
  - a. 23
  - b. -2
  - c.  $n^2 + 6n + 7$
3.
  - a.  $\frac{1}{9}$
  - b. 81
  - c.  $\sqrt{3}$
4.
  - a. -28
  - b. -8
  - c. -8
5.
  - a. Translate left 7
  - b. Reflect in the y-axis; Reflect in the x-axis
  - c. Translate up 4; Vertical stretch by a factor of 3.
6.
  - a. Translate left 10; Vertical shrink by a factor of  $\frac{1}{2}$ .
  - b. Reflect in the x-axis; Translate down 3; Vertical stretch by a factor of 2.
  - c. Translate right 6; Translate up 4.
7.
  - a.  $f(x) = |x-1| - 3$
  - b.  $f(x) = -2|x| + 4$
  - c.  $f(x) = -|x+2|$
  - d.  $f(x) = \frac{1}{2}|x|$
8.  $A(h) = (h)(h+6) = h^2 + 6h$

Homework 2.3 Solutions

1. Increasing interval(s):  $(-4, \infty)$   
 Decreasing interval(s):  $(-\infty, -4)$   
 Relative maximum(s): NA  
 Relative minimum(s):  $(-4, -1)$   
 x-intercept(s):  $(-6, 0), (-2, 0)$   
 y-intercept:  $(0, 3)$
2. Increasing interval(s):  $(-\infty, \infty)$   
 Decreasing interval(s): NA  
 Relative maximum(s): NA  
 Relative minimum(s): NA  
 x-intercept(s):  $(-5, 0)$   
 y-intercept:  $(0, 4)$
3. Increasing interval(s):  $(-2, 3)$   
 Decreasing interval(s):  $(-\infty, -2), (3, \infty)$   
 Relative maximum(s):  $(3, 1)$   
 Relative minimum(s):  $(-2, -4)$   
 x-intercept(s):  $(-6, 0), (2, 0), (4, 0)$   
 y-intercept:  $(0, -2)$
4. Increasing interval(s):  $(-\infty, -4), (-2, 0), (2, \infty)$   
 Decreasing interval(s):  $(-4, -2), (0, 2)$   
 Relative maximum(s):  $(-4, 1), (0, 1)$   
 Relative minimum(s):  $(-2, -1), (2, -1)$   
 x-intercept(s):  $(-5, 0), (-3, 0), (-1, 0), (1, 0), (3, 0)$   
 y-intercept:  $(0, 1)$
5. Increasing interval(s):  $(-\infty, \infty)$   
 Decreasing interval(s): NA  
 Relative maximum(s): NA  
 Relative minimum(s): NA  
 x-intercept(s):  $(-4, 0)$   
 y-intercept:  $(0, 2)$
6. Increasing interval(s): NA  
 Decreasing interval(s):  $(-\infty, -1), (-1, \infty)$   
 Relative maximum(s): NA  
 Relative minimum(s): NA  
 x-intercept(s):  $(1, 0)$   
 y-intercept:  $(0, 1)$
7.  $(-1, 0)$ ; Minimum
8.  $(3, 5)$ ; Maximum
9.  $(0, 8)$ ; Maximum
10.  $(-6, -4)$ ; Minimum
- ★ Maximum:  $(0, 4)$
11. Minimums:  $(-2, 0), (2, 0)$

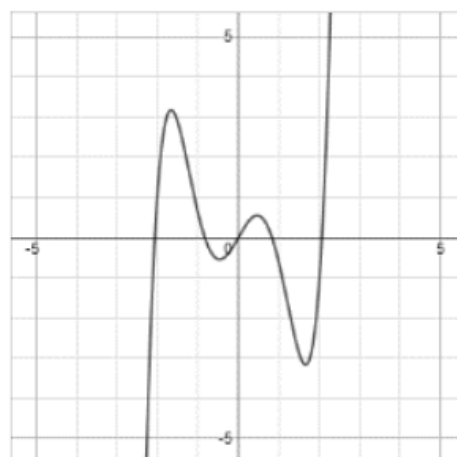


## Lesson 2.4 Objectives

I can identify features of functions including: classification as odd, even, or neither; and rate of change over a given interval.

### Odd Functions

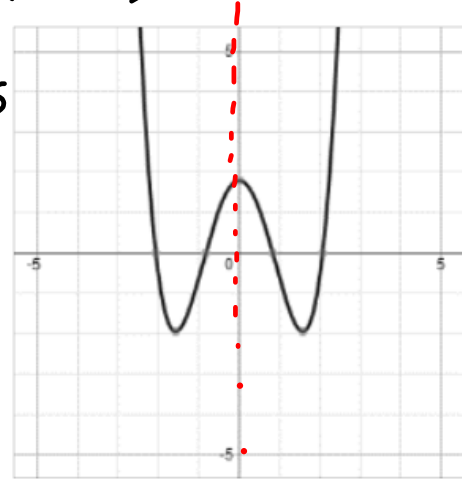
- All degrees of  $x$  are odd.
- Rotational symmetry about the origin.
- $-f(x) = f(-x)$



## Even Functions

$$x^2 + 3$$

- All degrees of  $x$  are even. *★ constants are even*
- Reflective symmetry about the  $y$ -axis.
- $f(x) = f(-x)$



If a function does not fit the conditions for either ODD or EVEN, it is NEITHER even or odd

A non-zero constant term  $c$  is considered an even degree of  $x$  since it can be written  $cx^0$ .

2)

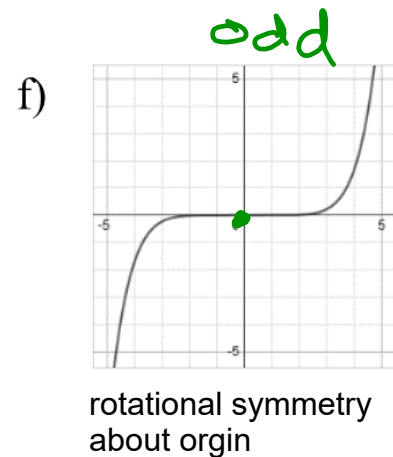
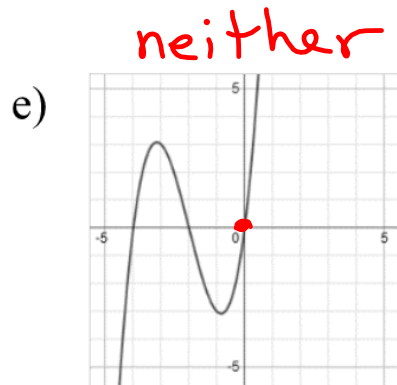
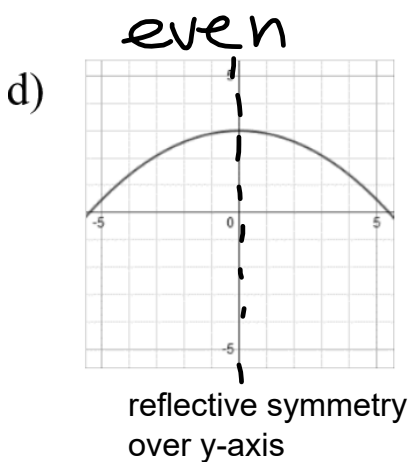
Determine if the functions are even, odd, or neither

a)  $f(x) = 3x^2$  even

b)  $f(x) = 7x^5 + 1x^0$  neither  
↙ odd
↘ even

c)  $f(x) = 2x^3 - 8x^1$  odd

Determine if the functions are even, odd, or neither



$$\text{Average rate of change} = \frac{\Delta y}{\Delta x} = \frac{\text{change in } y}{\text{change in } x}$$

$$\text{If you are given a domain interval } [a, b] \text{ with } x_1, x_2 = \frac{f(b) - f(a)}{b - a}$$

$$\text{If you are given 2 points on the function } (x_1, y_1) \text{ and } (x_2, y_2) = \frac{y_2 - y_1}{x_2 - x_1}$$

The average rate of change of an increasing EXPONENTIAL function will always be GREATER than an increasing QUADRATIC function as  $x \rightarrow \infty$

$$\frac{\text{EXP} > \text{QUAD} > \text{linear}}{e^x \quad x^2 \quad x}$$

For each function,  $a$ ,  $b$ ,  $c$ , and  $d$ , find the average rate of change on the interval  $[-3, 0]$ .

$x$	$a(x)$
-4	13
-3	11
-2	9
-1	7
0	5
1	3

$$m = \frac{f(0) - f(-3)}{0 - (-3)}$$

$$\frac{5 - 11}{0 + 3}$$

$$= \frac{-6}{3} = -2$$

$$b(x) = 2^{x+4}$$

$$\frac{f(0) - f(-3)}{0 - (-3)}$$

$$\frac{2^4 - 2^1}{3} = \frac{16 - 2}{3}$$

$$= \frac{14}{3}$$

$$c(x) = 4|x+2| \quad [-3, 0]$$

$$\frac{f(0) - f(-3)}{0 - (-3)} = \frac{8 - 4}{0 + 3} = \frac{4}{3}$$

$$f(0) = 4|0+2| = 4|2| = 8$$

$$f(-3) = 4|-3+2| = 4|-1| = 4(1) = 4$$

$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{-3 - (-2)}{-3 - 0}$$

$$= \frac{-3 + 2}{-3} = \frac{-1}{-3} = \frac{1}{3}$$